

# Three-Ball Contact Tutorial (AutoDesign)





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#### **Edition Note**

This document describes the release information of **RecurDyn V9R4**.

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# **Outline of Tutorial Sample A**





## Three-Ball Contact Problem

To explain the basic function of **AutoDesign**, let's solve a simple design problem. The design model consists of three balls. The yellow and the blue ball are fixed on ground. When the red ball is thrown with an initial velocity, the red ball should be contacted with the yellow ball and go through the blue ball as near as possible.

- **1. Model Definition**
- **2. Design Parameter Definition**
- **3. Analysis Response Definition**
- **4. Design Study**
- **5. Design Optimization**

Next, the refined optimization is explained to find more accurate results. This design uses the simulation results to solve the former design problem.

### **6. Refining the Design Formulation**



**Note**: If you change the file path at discretion, it can be located in any folder that you specify.



## Model Definition

The contact between the red ball and the yellow ball is defined but is not done between the red ball and blue ball, because the blue ball is just the target point. The design variables are the initial velocity of red ball along x-direction and the contact stiffness coefficient in the contact force between the red and the yellow balls. Now, for the red ball to pass the nearest way to the center of the blue ball, what can you define as the design objective and constraints?

### To do this, the design system is modeled as follows:



Figure A-1-1 MBD Model of the ball contact design problem

The below is the procedure for defining the balls, joint and contact force shown in Figure A-1- 1.

**1.** Make balls using '**Ellipsoid**' icon in the body module folder.

# Ellipsoid

Fixed

**2.** Fixed the Yellow ball and the Blue ball with ground using the '**Fixed**' joint in the joint module folder.



**3.** Define the contact force between the red ball and the yellow ball using the '**Sphere To Sphere**' contact in the contact module folder.



## Design Parameter Definition

#### Let's study the procedure for defining design parameters:

- $\alpha$ PV
- **1.** Define parametric values shown in Figure A-2-1.



Figure A-2-1 Parametric value definition

**2.** Link the '**InitialVX**' with the x direction initial velocity of the red ball body shown in Figure A-2-2.



Figure A-2-2 Link the '**InitialVX'**

**3.** Link the '**K**' with the stiffness coefficient of the contact force between the red ball and the yellow ball shown in Figure A-2-3.



Figure A-2-3 Link the stiffness '**K**'

 $\alpha$ h Parameter **4.** Define the design parameters from parametric values using the '**Design Parameter**' command in the '**AutoDesign'** toolkit shown in Figures A-2-4 and A-2-5. First, you push 'Create' button to define the design parameters as Figure A-2-4. In Figure A-2-5, you should link the design parameters to the parametric values that were defined in Figure A-2-1. The initial values are the current parametric values defined in Figure A-2-1. You should define the lower and the upper bounds on the design variable. This represents that the optimization process should change the design values within these bounds during iterations. After you create the design parameters, you check the active design parameters for this design problem.

		Design Parameter List									
	<b>Design Parameter</b>										
м.,	Name	Type	Prop.	Descripti	Curr	LB	<b>UB</b>	Design Cost	DP Form   DV		
	DP1	<b>Direct</b>		Initial VX	2700.	15	50		Value	⊮	

Figure A-2-4 Check '**DV'** check box



Figure A-2-5 Define '**DP1**' and '**DP2**'



## Analysis Response Definition

The design goal is that the center of the red ball passes the nearest way from the center of the blue ball, the target point. You need to define the performance indexes for solving the optimization problem. In **AutoDesign**, performance indexes are objectives and constraints in design optimization, which are composed of analysis responses. Then, in order to define the performance index, analysis responses are defined first. The procedure of defining analysis responses is explained as:



Define **Expressions**. Each expression is defined shown in the Figures A-3-2, A-3-3, and A-3- 4, sequentially.

	<b>Expression List</b>					
<b>Expressions</b>						
<b>No</b>	Name	Expression		Value	Comment	-
	Ex1	DM(1,2)	Ė	3138.47		
	Ex2	CONTACT(1,0,1,2)	Ė	$\mathbf 0$		

Figure A-3-1 Expression List





Figure A-3-3 Detailed Definition of Expression Ex2



Figure A-3-4 Detailed Definition of Expression Ex3



Register expressions for analysis response shown in Figure A-3-5. Other figures are representing the dialogue of each analysis response. Define the **Analysis Response** using the **'Analysis Reponse'** command in the '**AutoDesign'** toolkit. The detailed information for each analysis response is shown in Figure A-3-6. Also, their physical relations are shown in Figure A-3-7.

	Analysis Response List						
	<b>Analysis Response</b>						
<b>No</b>	Name	Type	Pr	Description	<b>Treatment</b>	PI	
	AR1	<b>Basic</b>		Distance between Red Ball &	Min Value	$\bar{ }$	
	AR <sub>2</sub>	<b>Basic</b>		Contact Force between Red B	Max Value	☞	
	AR3	<b>Basic</b>		Distance between Red BAII &	Min Value	⊮	

Figure A-3-5 Analysis Response List



Figure A-3-6 The detailed information for three analysis responses



Figure A-3-7 Three analysis responses in the model



## Design Study

Before you start to solve this optimization problem, it needs to know the relationship between design variables and analysis responses or the correlation between analysis responses. To get that kind of information, you need the effect analysis from design of experiments. **AutoDesign** provides such functions as effect analysis, correlation analysis and even design variable screening in Design Study menu. Design Study is composed of six sub-menus listed in Table A-4-1.



Table A-4-1 Description of sub-menu in Design Study

### Basic Procedure for Design Study



In order to design study such as effect analysis, screening variables and correlation analysis, you select the DOE method and define the level for each variable and perform the simulation of **RecurDyn**. First, these procedures are explained as:

**1.** In the sub-menu of design variables, select '**Bose's Orthogonal Design**' in DOE methods, and set the level of the study as '**5**'. Then, one defines the required runs as 25. This method is a strength-II orthogonal array design. For more information, one may refer to the theoretical manual of **AutoDesign**.



Figure A-4-1 Define DOE method for design study

**2.** Confirm the Performance index that is checked in Analysis Responses.

Design Study				
Design Variable	Performance Index	Simulation Control	Effect Analysis   Screening Variables	<b>Correlation Analysis</b>
PI	AR			Description
	AR1			Distance between Red Ball & Blue Ball
	AR <sub>2</sub>			Contact Force between Red Ball & Yellow Ball
	AR3			Distance between Red Ball & Yellow Ball

Figure A-4-2 The selected PI list for design study

**3.** In the sub-menu of simulation control, define analysis setting shown in Figures A-4-4 and A-4-5. This setting is the same as that in RD analysis. If you increase the accuracy of effect analysis and optimization results, it is recommended that the **plot multiplier factor** should be **'1.0'** and increase the number of steps. After setting the options, push the **OK** button. After setting them, push the Execution button. Then, **RecurDyn** is analyzed for the given number of trials.



Figure A-4-3 Simulation Control page



Figure A-4-4 General analysis setting



Figure A-4-5 Integrator parameter setting

- **4.** After all analyses are completed, one can select the effect analysis, correlation analysis and screening design variables.
- **5.** Now, select the effect analysis menu. Effect analysis gives the relation between one performance index and all design variables.

### **Effect Analysis**

Figure A-4-6 shows the effect analysis menu. Let's study the effect analysis procedure.

Select the performance index in PI row. Then check the design variables to see the effect analysis for the selected PI. Then, push DRAW button. Figure A-4-7 shows the effect analysis between PI\_1 and design variables. This shows that DV1 is more nonlinear than DV2 in the distance between red ball and blue ball.

	Design Study								
	Design Variable	Performance Index	<b>Simulation Control</b>		<b>Effect Analysis</b>	Screening Variables	<b>Correlation Analysis</b>		
PI		1: AR1(DM(1,2)) <b>Effect Values and Variation</b>						 Draw 	$\mathbf{r}$
	<b>DV</b>	Level1	Level <sub>2</sub>	Level3	Level4	Level <sub>5</sub>	Variation	<b>Effect Value</b>	
		2.208152655	1.358839406	0.487655979	0.652289790	0.293062168		V	
		0.808903863.	1.036337385	1.051277050	1.052378731	1.051102968			

Figure A-4-6 Sub-menu for effect analysis



Figure A-4-7 Effect analysis result for the first PI

Similarly, you can see the effect analysis for PI\_2, which is shown in Figure A-4-8. For the 4th and 5th levels of DV1, the contact forces are 'zero'. This represents that two balls are not contacted for those cases. It is noted that this discontinuity makes the accuracy of metamodel to be worse.



Figure A-4-8 Effect analysis result for the second PI

Finally, you can see the effect analysis for PI\_3, which is shown in Figure A-4-9. This represents the distance between red and yellow balls. Unlike Figure A-4-8, this shows a continuous result even though two balls didn't contact for 4th and 5th levels of DV1. This represents that PI\_3 is suitable to define the contact constraint in the design optimization.



Figure A-4-9 Effect analysis result for the third PI

The explanation of effect analysis is completed. However, you have a question for the minimization or maximization combinations shown in Figure A-4-10.



Figure A-4-10 Selection of minimization or maximization combination

Suppose that you select the third PI. Then, you see the effect analysis result shown in Figure A-4-9. Then, Figure 4-10 shows the design variable combination for minimizing PI\_3 and maximizing PI\_3. If you need the confirmation for minimum or maximum set, then select one of them and push simulation button in Figure A-4-10 menu.

### Screening Variables

Figure A-4-11 shows the menu for screening variables. First, you can see the scatter points. This represents the design variables. In this problem, there are only two design variables. Thus, variable screening is not required but we study only the screening variable method.

**1.** First, select the first performance index, **PI\_1**. Figure A-4-11 shows that two design variables have severely different effectiveness. Now, you need to know which variable is effective for PI\_1.

**2.** Define the cutoff values as 1.0 and push **Apply** button. You can see Figure A-4-12. Then, push the **Screening DV** button. Figure A-4-13 shows the screening result. It shows that design variable DV1 (or DP1) is more effective than DV2.



Figure A-4-11 Sub-menu for screening variables



Figure A-4-12 Defining the cutoff value for screening variables



Figure A-4-13 Screened result for the first performance index

**3.** Next, change the performance index **AR3**. Then, define the cutoff value as 12. Perform the similar procedure in step 2. Then you can see the result shown in Figure A-4-14. In the figure, Current represents the screening results for PI\_3. Total represents the union of screening results for PI\_1 and PI\_3. If you push **Save** button, only active design variables (marked 'on') are remained in New Model or Current Model.



Figure A-4-14 Screened result for the third performance index

### Correlation Analysis

Figure A-4-15 shows the menu for correlation analysis. This shows the relation between two selected ARs from the analysis results. If you see the relation between the first PI and the third PI, check Horizontal Axis as PI\_1 and Vertical Axis as PI\_3 and push Draw button. Then, you can see the correlation result shown in Figure A-4-16. Figure A-4-16 shows that they have no trend or slightly reverse trend.



Figure A-4-15 Sub-menu for correlation analysis



Figure A-4-16 Correlation result between PI\_1 and PI\_3



## Design Optimization

#### Let's remind the following design problem:

Find the initial velocity of red ball along x-direction and the contact stiffness between red and yellow balls for red ball to hit the blue ball after red ball hit yellow ball.



Next process is for defining the design option and executing the optimization analysis. The first step is to define the design variables shown in the Figure A-5-1. This can start using the '**Design Optimization**' command in the '**Auto Design**' toolkit.



**1.** In **Design Variable** menu, the selected DPs are listed. In this menu, DP can be design variable or constant during optimization process. If you define a DP as constant, you should define its constant value.

	Design Optimization							
Design Variable		Performance Index   Optimization Control   Result Sheet   Summary Sheet						
DV	<b>DP</b>	<b>Description</b>	Current	LB	<b>UB</b>	Type	Value	
	DP <sub>1</sub>	Initial VX	2700.	1500.	5000.	Variable	$\mathbf{0}$	
	DP <sub>2</sub>	<b>Stiffness K</b>	10.	1.	20.	Variable	0.	

Figure A-5-1 Definition of design variables

**2.** The next process is to define the performance indexes in Figure A-5-2, which is named as 'performance index' of the dialog of Figure A-5-1. **Performance Index** is a design optimization formulation part. Figure A-5-3 shows the mathematical definition for design optimization. Let's discuss the optimization formulation in Figure A-5-2. In the first performance index, choose **AR1** and define it as objective. Also, select the design goal as minimization and define its weighting coefficient as **1.0**. In the second performance index, add one inequality constraint as '**AR1 =< 100'**. In the third performance index, add one inequality constraint as '**AR3 =< 0'**, In the last performance index, choose **AR2** and define it as objective. Unlike AR1, the design goal is defined as maximization and its weight coefficient is defined as **1**.

	Design Variable	Performance Index			Optimization Control   Result Sheet	<b>Summary Sheet</b>		
PI	<b>Use</b>	AR.		<b>Description</b>	<b>Definition</b>	Goal		Weight/Limit Value
	◡	AR1		Distance between R	Objective	<b>MIN</b>	$\overline{\phantom{a}}$	1.
2	✓	AR1		Distance between R	Constraint	LE		100.
٩	$\overline{\phantom{a}}$	AR3		Distance between R	Constraint	LE.		0.
Δ	◡	AR <sub>2</sub>	▼	Contact Force betw	Objective	<b>MAX</b>		1.

Figure A-5-2 Definition of performance indexes



Figure A-5-3 Design optimization formulation

**3.** Check the analysis setting by clicking the **Analysis Setting** button. In order to reduce the numerical error, we increase the number of time steps shown in right. If you increase the resolution of optimization solution, then increase the number of steps. In refining the design optimization, we will show more accurate design by only increasing the value.



**4.** Define the option of optimization control and execute analysis shown in the Figure A-5-4. The analysis setting is the same that of Design Study. Finally, if you push the optimization button, you can see the summary of the design optimization formulation shown in Figure A-5-5. Then, check your formulation. If you see some mistakes, then push the **Cancel** button and correct the mistakes. Otherwise, push the **Execution** button. Then, **AutoDesign** runs until convergence criteria are satisfied or maximum iteration is reached. During optimization process, you can see the analysis results in the **Simulation History** menu.



Figure A-5-4 Control option definition for optimization and analysis

<b>No</b>	<b>DV</b>	Description	Current	LB.	<b>UB</b>	Type	Value
1.	DP1	Initial VX	2700.	1500.	5000.	Variable	$\mathbf{0}$ .
$\overline{2}$	DP <sub>2</sub>	Stiffness K	10.	1.	20.	Variable	0.
	<b>Performance Indexes</b>						
<b>No</b>		<b>AR</b>	Description		<b>Definition</b>	Goal	Weight/Limit Value
1		AR1	Distance between Red Ball		Objective	<b>MIN</b>	1.
2		AR1	Distance between Red Ball		Constraint	LE:	100.
3		AR3	Distance between Red Ball		Constraint	LE	$\overline{0}$ :
4		AR <sub>2</sub>	Contact Force between Red		Objective	<b>MAX</b>	1.
	Meta - Model						
	<b>Initial DOE Method</b>				Incomplete Small Composite Design -2		
	Meta-Model Method				Radial Basis Functions Model(Multi-Quadratic)		
	<b>Polynominal Type</b>				Auto		
	<b>Trial No</b>				5		

Figure A-5-5 Summary of design optimization formulation

**5.** If **AutoDesign** is completed, then you can see the convergence results in **Result Sheet**. Figure A-5-6 shows the optimization results. In **RecurDyn**, the final value of AR1 is **0.732(mm)** after **8** iterations. Figure A-5-7 shows the trajectory of red ball for **SAO 8**.



Figure A-5-6 Convergence history



Figure A-5-7 Animation of the final design

*Thanks for participating in this tutorial!*